



Derivative Rules - Quotient Rule Positive Fractional Powers as Radical to Derivative

1 Find the derivative $f'(x)$ using the quotient rule.

$$f(x) = \frac{5\sqrt[3]{x^2} - 5}{2x + 3}$$

$$A \quad f'(x) = \frac{(\frac{10}{3}x^{-\frac{1}{3}})(2x+3) - (5x^{\frac{2}{3}} - 5)(2)}{(2x+3)^2}$$

$$C \quad f'(x) = \frac{(5x^{\frac{2}{3}} - 5)(2) - (\frac{10}{3}x^{-\frac{1}{3}})(2x+3)}{(2x+3)^2}$$

$$B \quad f'(x) = \frac{(\frac{10}{3}x^{-\frac{1}{3}})(2x+3) - (5x^{\frac{2}{3}} - 5)(2)}{(2x+3)}$$

$$D \quad f'(x) = \frac{(\frac{10}{3}x^{-\frac{1}{3}})(2x+3) + (5x^{\frac{2}{3}} - 5)(2)}{(2x+3)^2}$$

2 Find the derivative $f'(x)$ using the quotient rule.

$$f(x) = \frac{4\sqrt[3]{x} + 7}{-3x^2}$$

$$A \quad f'(x) = \frac{(4x^{\frac{1}{3}} + 7)(-6x) - (\frac{4}{3}x^{-\frac{2}{3}})(-3x^2)}{(-3x^2)^2}$$

$$C \quad f'(x) = \frac{(\frac{4}{3}x^{-\frac{2}{3}})(-3x^2) + (4x^{\frac{1}{3}} + 7)(-6x)}{(-3x^2)^2}$$

$$B \quad f'(x) = \frac{(\frac{4}{3}x^{-\frac{2}{3}})(-3x^2) - (4x^{\frac{1}{3}} + 7)(-6x)}{(-3x^2)}$$

$$D \quad f'(x) = \frac{(\frac{4}{3}x^{-\frac{2}{3}})(-3x^2) - (4x^{\frac{1}{3}} + 7)(-6x)}{(-3x^2)^2}$$

3 Find the derivative $f'(x)$ using the quotient rule.

$$f(x) = \frac{2\sqrt[3]{x^4} - 4}{2x^2}$$

$$A \quad f'(x) = \frac{(2x^{\frac{4}{3}} - 4)(4x) - (\frac{8}{3}x^{\frac{1}{3}})(2x^2)}{(2x^2)^2}$$

$$C \quad f'(x) = \frac{(\frac{8}{3}x^{\frac{1}{3}})(2x^2) + (2x^{\frac{4}{3}} - 4)(4x)}{(2x^2)^2}$$

$$B \quad f'(x) = \frac{(\frac{8}{3}x^{\frac{1}{3}})(2x^2) - (2x^{\frac{4}{3}} - 4)(4x)}{(2x^2)^2}$$

$$D \quad f'(x) = \frac{(\frac{8}{3}x^{\frac{1}{3}})(2x^2) - (2x^{\frac{4}{3}} - 4)(4x)}{(2x^2)}$$

4 Find the derivative $f'(x)$ using the quotient rule.

$$f(x) = \frac{-4\sqrt[3]{x^2} - 4}{-5x}$$

$$A \quad f'(x) = \frac{(-4x^{\frac{2}{3}} - 4)(-5) - (-\frac{8}{3}x^{-\frac{1}{3}})(-5x)}{(-5x)^2}$$

$$C \quad f'(x) = \frac{(-\frac{8}{3}x^{-\frac{1}{3}})(-5x) - (-4x^{\frac{2}{3}} - 4)(-5)}{(-5x)}$$

$$B \quad f'(x) = \frac{(-\frac{8}{3}x^{-\frac{1}{3}})(-5x) - (-4x^{\frac{2}{3}} - 4)(-5)}{(-5x)^2}$$

$$D \quad f'(x) = \frac{(-\frac{8}{3}x^{-\frac{1}{3}})(-5x) + (-4x^{\frac{2}{3}} - 4)(-5)}{(-5x)^2}$$

5 Find the derivative $f'(x)$ using the quotient rule.

$$f(x) = \frac{3\sqrt[3]{x^4} + 4}{4x}$$

$$A \quad f'(x) = \frac{(4x^{\frac{4}{3}})(4x) + (3x^{\frac{4}{3}} + 4)(4)}{(4x)^2}$$

$$C \quad f'(x) = \frac{(3x^{\frac{4}{3}} + 4)(4) - (4x^{\frac{4}{3}})(4x)}{(4x)^2}$$

$$B \quad f'(x) = \frac{(4x^{\frac{4}{3}})(4x) - (3x^{\frac{4}{3}} + 4)(4)}{(4x)^2}$$

$$D \quad f'(x) = \frac{(4x^{\frac{4}{3}})(4x) - (3x^{\frac{4}{3}} + 4)(4)}{(4x)}$$

6 Find the derivative $f'(x)$ using the quotient rule.

$$f(x) = \frac{-2\sqrt{x} - 2}{2x^2 + 6}$$

$$A \quad f'(x) = \frac{(-x^{-\frac{1}{2}})(2x^2 + 6) - (-2x^{\frac{1}{2}} - 2)(4x)}{(2x^2 + 6)^2}$$

$$C \quad f'(x) = \frac{(-2x^{\frac{1}{2}} - 2)(4x) - (-x^{-\frac{1}{2}})(2x^2 + 6)}{(2x^2 + 6)^2}$$

$$B \quad f'(x) = \frac{(-x^{-\frac{1}{2}})(2x^2 + 6) + (-2x^{\frac{1}{2}} - 2)(4x)}{(2x^2 + 6)^2}$$

$$D \quad f'(x) = \frac{(-x^{-\frac{1}{2}})(2x^2 + 6) - (-2x^{\frac{1}{2}} - 2)(4x)}{(2x^2 + 6)^2}$$

7 Find the derivative $f'(x)$ using the quotient rule.

$$f(x) = \frac{3\sqrt{x} + 6}{-5x + 7}$$

$$A \quad f'(x) = \frac{(\frac{3}{2}x^{-\frac{1}{2}})(-5x+7) - (3x^{\frac{1}{2}} + 6)(-5)}{(-5x+7)^2}$$

$$C \quad f'(x) = \frac{(3x^{\frac{1}{2}} + 6)(-5) - (\frac{3}{2}x^{-\frac{1}{2}})(-5x+7)}{(-5x+7)^2}$$

$$B \quad f'(x) = \frac{(\frac{3}{2}x^{-\frac{1}{2}})(-5x+7) + (3x^{\frac{1}{2}} + 6)(-5)}{(-5x+7)^2}$$

$$D \quad f'(x) = \frac{(\frac{3}{2}x^{-\frac{1}{2}})(-5x+7) - (3x^{\frac{1}{2}} + 6)(-5)}{(-5x+7)}$$

8 Find the derivative $f'(x)$ using the quotient rule.

$$f(x) = \frac{5\sqrt[3]{x} + 3}{5x}$$

$$A \quad f'(x) = \frac{(\frac{5}{3}x^{-\frac{2}{3}})(5x) + (5x^{\frac{1}{3}} + 3)(5)}{(5x)^2}$$

$$C \quad f'(x) = \frac{(\frac{5}{3}x^{-\frac{2}{3}})(5x) - (5x^{\frac{1}{3}} + 3)(5)}{(5x)^2}$$

$$B \quad f'(x) = \frac{(\frac{5}{3}x^{-\frac{2}{3}})(5x) - (5x^{\frac{1}{3}} + 3)(5)}{(5x)}$$

$$D \quad f'(x) = \frac{(5x^{\frac{1}{3}} + 3)(5) - (\frac{5}{3}x^{-\frac{2}{3}})(5x)}{(5x)^2}$$